

# Exploring Quantum Properties of Propagating Microwaves with Superconducting Circuits

Andreas Wallraff (*ETH Zurich*)

[www.qudev.ethz.ch](http://www.qudev.ethz.ch)

Team: A. Abdumalikov, M. Baur, S. Berger, C. Eichler, A. Fedorov, S. Filipp, J. Fink, T. Frey, C. Lang, J. Mlynek, M. Oppliger, M. Pechal, G. Puebla-Hellmann, K. Reim, Y. Salathe, L. Steffen, T. Thiele, A. van Loo (*ETH Zurich*)

Collaborations:

A. Blais (*Sherbrooke, Canada*)

M. da Silva (*Raytheon, USA*)

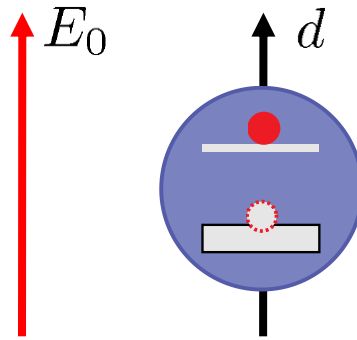
K. Ensslin, F. Merkt, V. Wood  
(*ETH Zurich*)



Eidgenössische Technische Hochschule Zürich SWISS NATIONAL SCIENCE FOUNDATION  
Swiss Federal Institute of Technology Zurich

# Controlling the Interaction of Photons and Qubits

challenging on the level of single particles

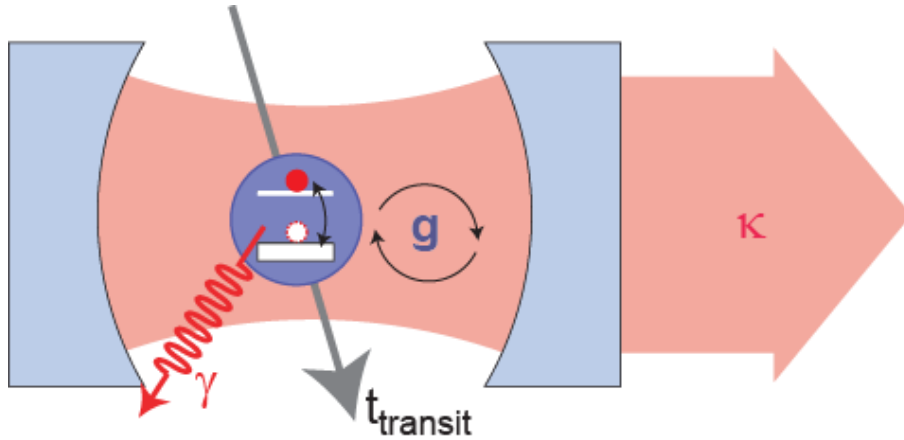


- dipole moment  $d$  in microscopic systems (usually small  $\sim ea_0$ )
- single photon fields  $E_0$  (small in 3D)
- photon/qubit interaction  $\hbar g \sim dE_0$  (usually small)

What to do?

- confine qubit and photon in a cavity (cavity QED)
- engineer qubit/light interaction in solid state circuits

# Cavity QED with Superconducting Circuits



coherent interaction of photons with quantum two-level systems ...

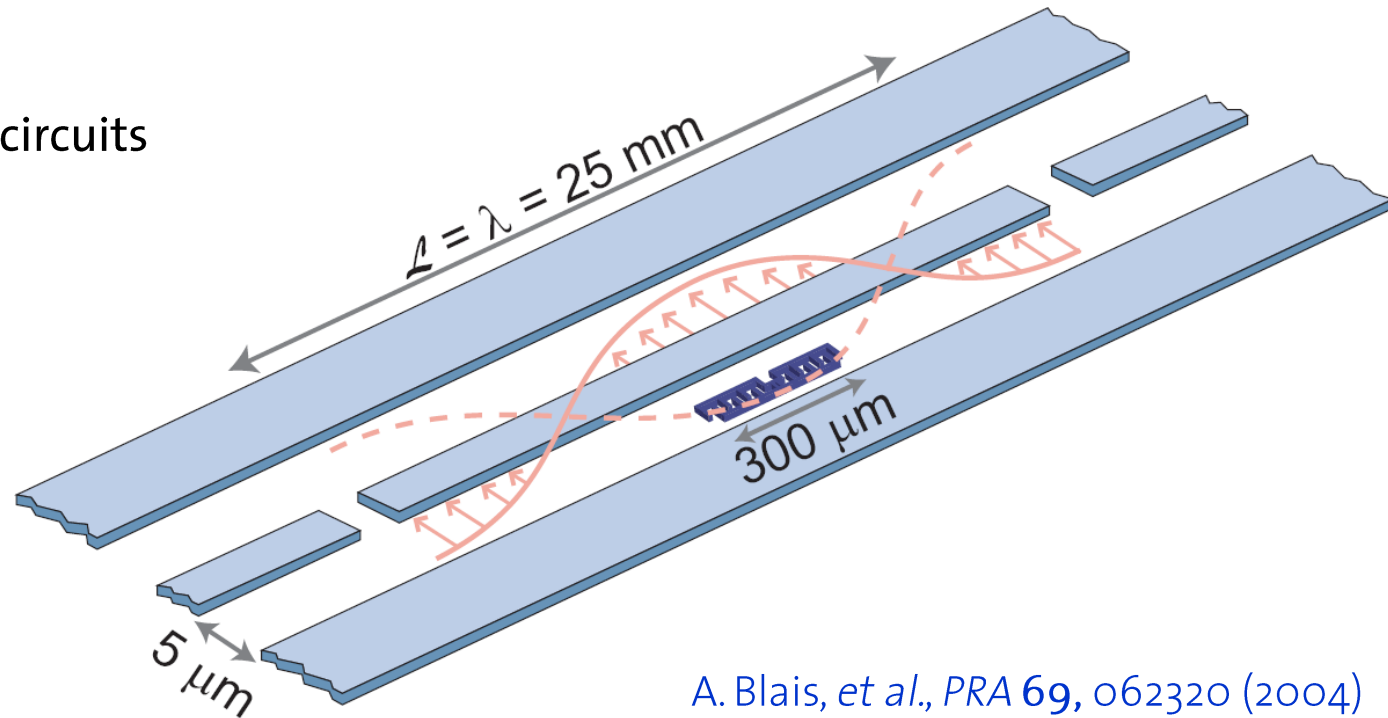
J. M. Raimond *et al.*, *Rev. Mod. Phys.* **73**, 565 (2001)

S. Haroche & J. Raimond, *oup Oxford* (2006)

J. Ye., H. J. Kimble, H. Katori, *Science* **320**, 1734 (2008)

... in superconducting circuits

circuit quantum electrodynamics



A. Blais, *et al.*, *PRA* **69**, 062320 (2004)

A. Wallraff *et al.*, *Nature (London)* **431**, 162 (2004)

R. J. Schoelkopf, S. M. Girvin, *Nature (London)* **451**, 664 (2008)



# Resonant Vacuum Rabi Mode Splitting ...

... with one photon ( $n = 1$ ):

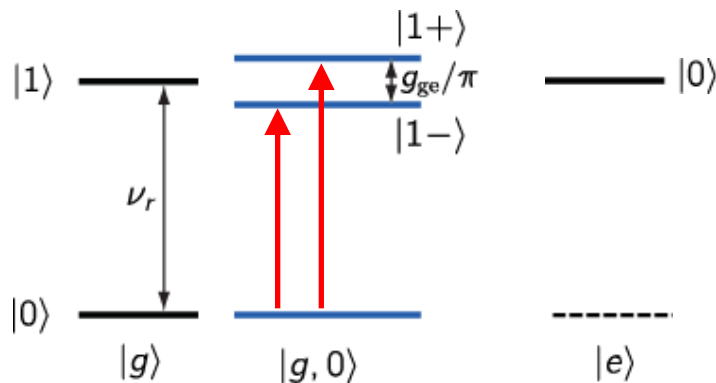
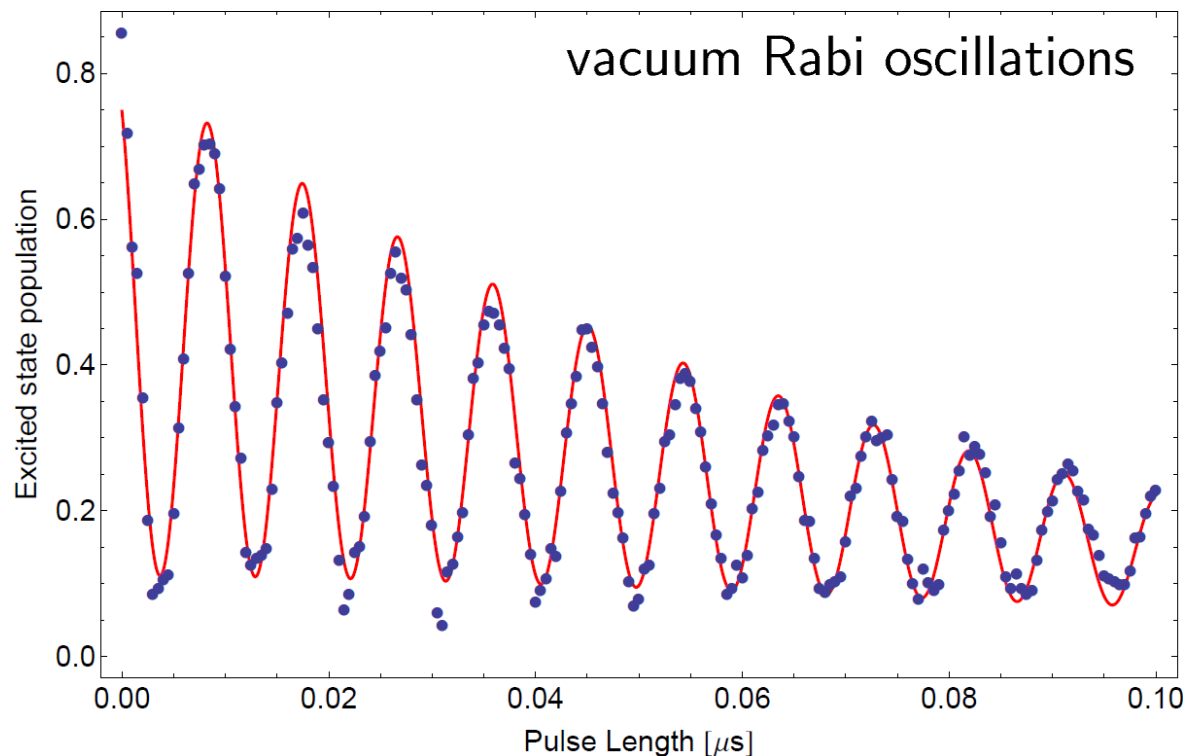
very strong coupling:

vacuum Rabi oscillations

$$g_{ge}/\pi = 308 \text{ MHz}$$

$$\kappa, \gamma < 1 \text{ MHz}$$

$$g_{ge} \gg \kappa, \gamma$$



forming a 'molecule' of a qubit and a photon

first demonstration in a solid: A. Wallraff et al., *Nature (London)* **431**, 162 (2004)

this data: J. Fink et al., *Nature (London)* **454**, 315 (2008)

R. J. Schoelkopf, S. M. Girvin, *Nature (London)* **451**, 664 (2008)

# Quantum Physics with Circuit QED ... some examples

## Vacuum Rabi Mode Splitting

A. Wallraff *et al.*, *Nature* **431**, 162 (2004)

## Coherent Flux-Qubit / SQUID Coupling

I. Chiorescu *et al.*, *Nature* **431**, 159 (2004)

## Quantum AC-Stark Shift

D. Schuster *et al.*, *Nature* **445**, 515 (2007)

## Lamb Shift

A. Fragner *et al.*, *Science* **322**, 1357 (2008)

## Fock and Arbitrary Photon States

M. Hofheinz *et al.*, *Nature* **454**, 310 (2008)

M. Hofheinz *et al.*, *Nature* **459**, 546 (2009)

## Root n Nonlinearity

J. Fink *et al.*, *Nature* **454**, 315 (2008)

## Two Photon Nonlinearities

F. Deppe *et al.*, *Nat. Phys.* **4**, 686 (2008)

## Parametric Amplification

Castellanos-Beltran *et al.*, *Nat. Phys.* **4**, 928 (2008)

## Super Splitting and Root n Nonlinearity

L. Bishop *et al.*, *Nat. Phys.* **5**, 105 (2009)

## Ultrastrong Coupling

T. Niemczyk *et al.*, *Nat. Phys.* **6**, 772 (2010)

## Single Photon Source

A. Houck *et al.*, *Nature* **449**, 328 (2007)

## Single Qubit MASER

O. Astafiev *et al.*, *Nature* **449**, 588 (2007)

## Single Qubit Resonance Fluorescence

O. Astafiev *et al.*, *Science* **327**, 840 (2010)

## QND Measurement of Single Photon

B. Johnson *et al.*, *Nat. Phys.* **6**, 663 (2010)

## Correlation Function Measurements

D. Bozyigit *et al.*, *Nat. Phys.* **7**, 154 (2011)

## Cooling and Amplification

M. Grajcar *et al.*, *Nat. Phys.* **4**, 612 (2008)

## Quantum Algorithms & Entangled States

L. DiCarlo *et al.*, *Nature* **460**, 240 (2009)

L. DiCarlo *et al.*, *Nature* **467**, 574 (2010)

A. Fedorov *et al.*, *Nature* **481**, 170 (2012)

M. Reed *et al.*, *Nature* **481**, 382 (2012)

## Quantum Bus

M. Sillanpaa *et al.*, *Nature* **449**, 438 (2007)

H. Majer *et al.*, *Nature* **449**, 443 (2007)

M. Mariani *et al.*, *Nat. Phys.* **7**, 287 (2011)

M. Mariani *et al.*, *Science* **334**, 61 (2011)

# Quantum Optics with Propagating Microwaves

quantum optics in the visible:

- single photon sources
- beam splitters
- photon counters

o.k. at optical frequencies

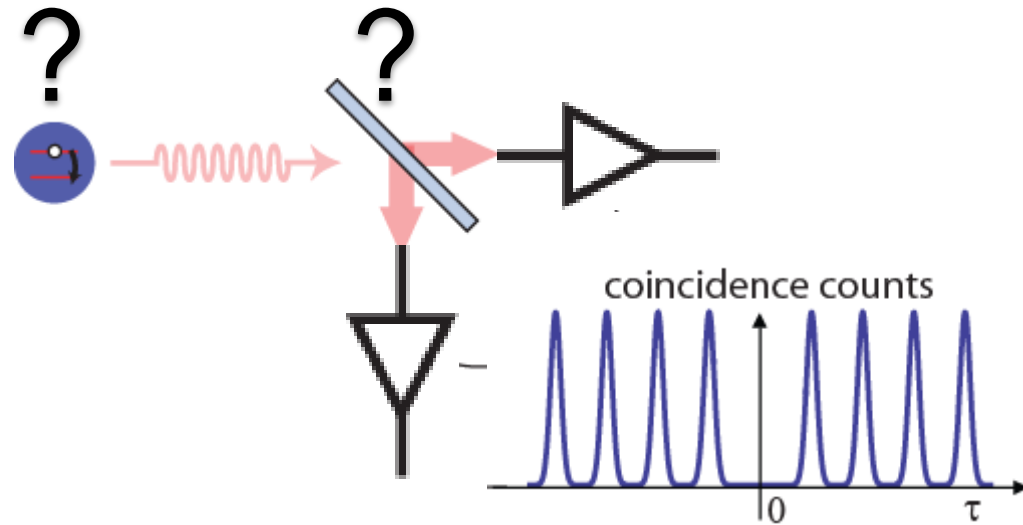
But in the microwave domain?

- smaller photon energy ...

$$\frac{\nu_{\text{opt}}}{\nu_{\mu\text{w}}} = \frac{500 \text{ THz}}{5 \text{ GHz}} = 10^5$$

- ... requires lower operating temperature

$$\frac{h}{k_B} 5 \text{ GHz} = 240 \text{ mK}$$



instead:

- linear amplifiers
- signal processing

Here:

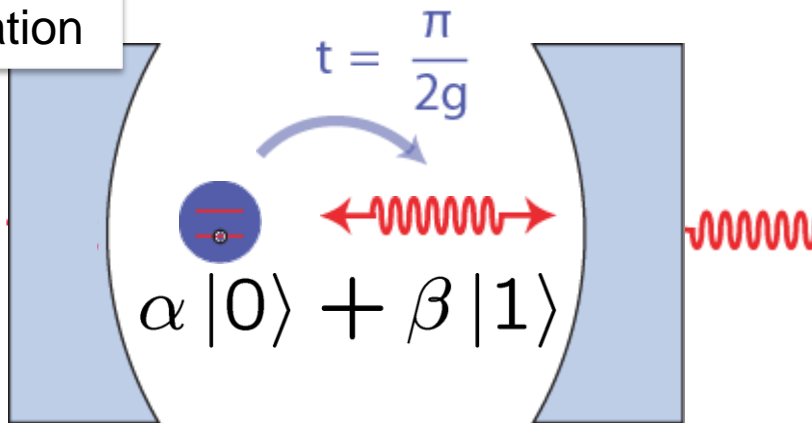
- correlation function msrmnts
- single photon tomography
- qubit/photon entanglement

J. Gabelli et al., *Phys. Rev. Lett.* **93**, 056801 (2004)  
E. P. Menzel et al., *Phys. Rev. Lett.* **105**, 100401 (2010)  
M. P. da Silva et al., *Phys. Rev. A* **82**, 043804 (2010)

# On-Demand Pulsed Single Photon Source

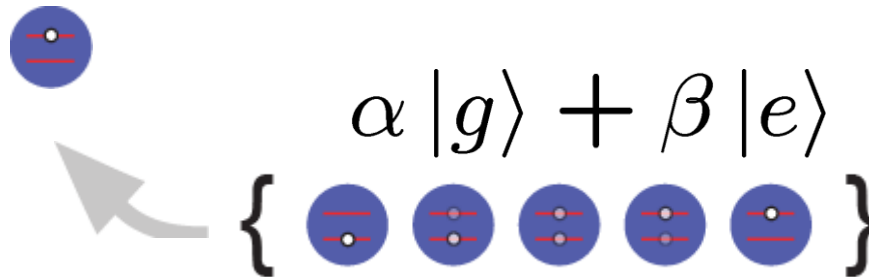
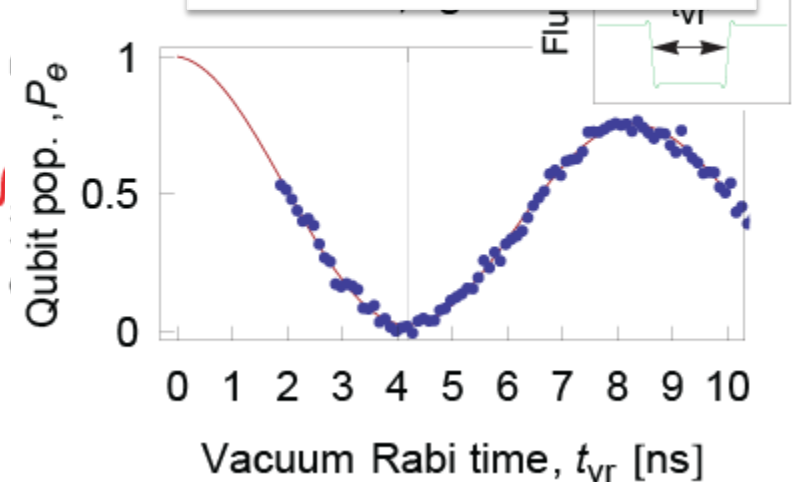
## Step 2:

Map qubit state to resonator by  $\pi/2$  vacuum Rabi oscillation



## Step 3:

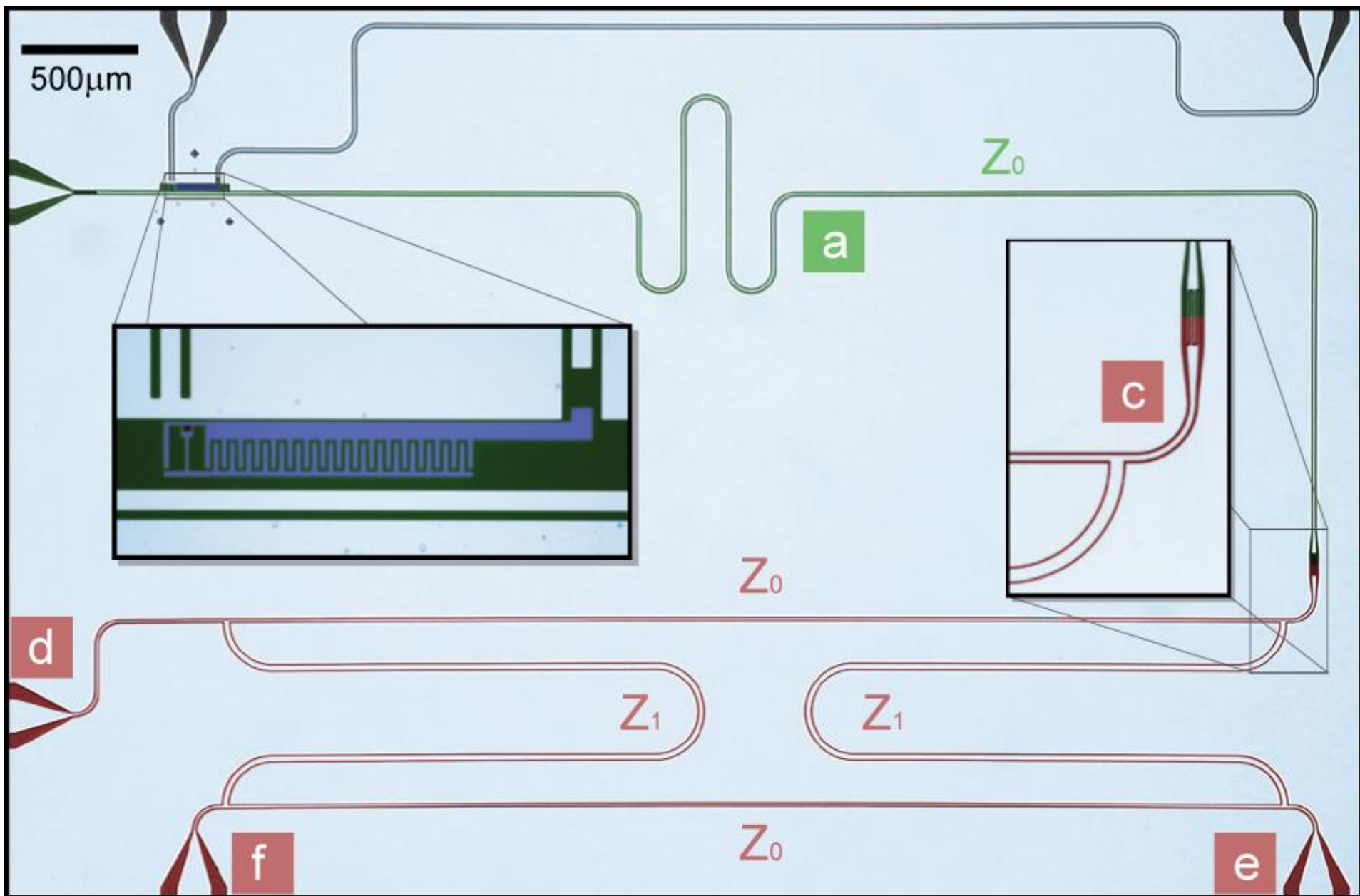
Measure at the output using linear amplifier and signal processing hardware



## Step 1:

Prepare qubit state by Rabi oscillation

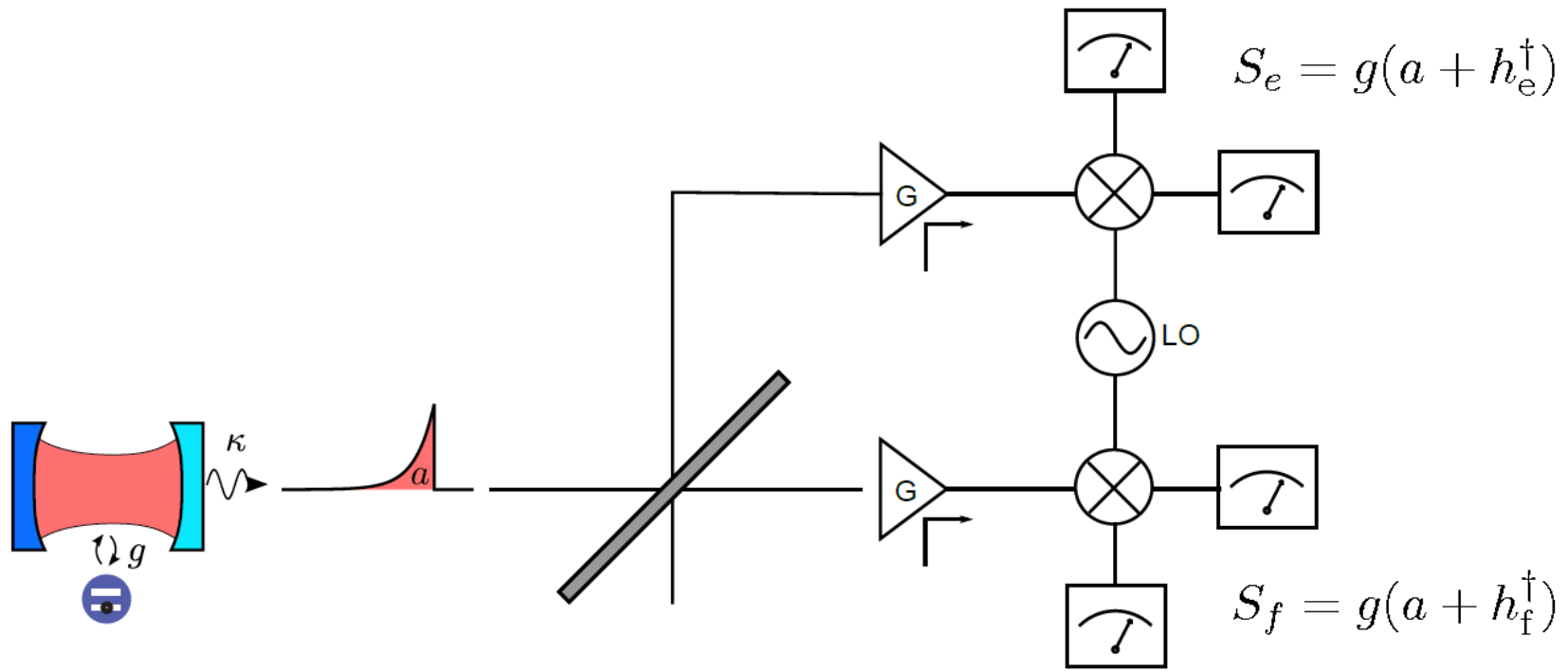
# Single Sided Cavity and Beam Splitter







# Schematic of Measurement Setup



$$g \equiv \sqrt{G/2}$$

$h_e, h_f$  effective noise modes

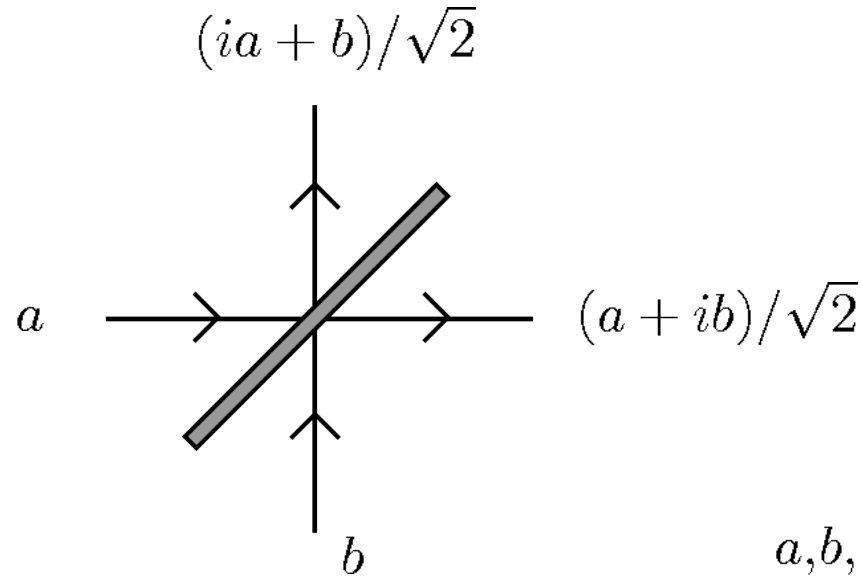
generalization of accessible expectation values:

$$\langle (S_e^\dagger)^n S_f^m \rangle = g^{n+m} \langle (a^\dagger)^n a^m \rangle$$

- M. P. da Silva et al., *PRA* **82**, 043804 (2010)
- D. Bozyigit et al., *Nat. Phys.* **7**, 154 (2011)
- S. L. Braunstein et al., *PRA* **43**, 1153 (1991)
- G. S. Argawal et al., *PRA* **49**, 2 (1994)

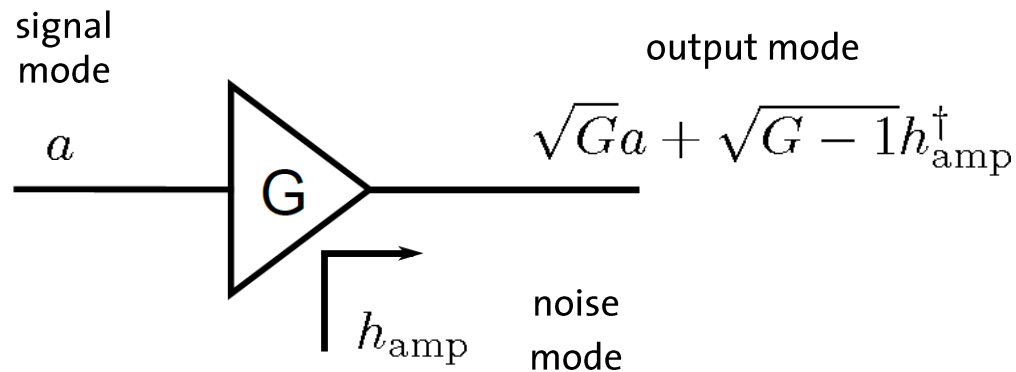
# Detection Scheme using Beam Splitters, Amplifiers ...

beam splitter:



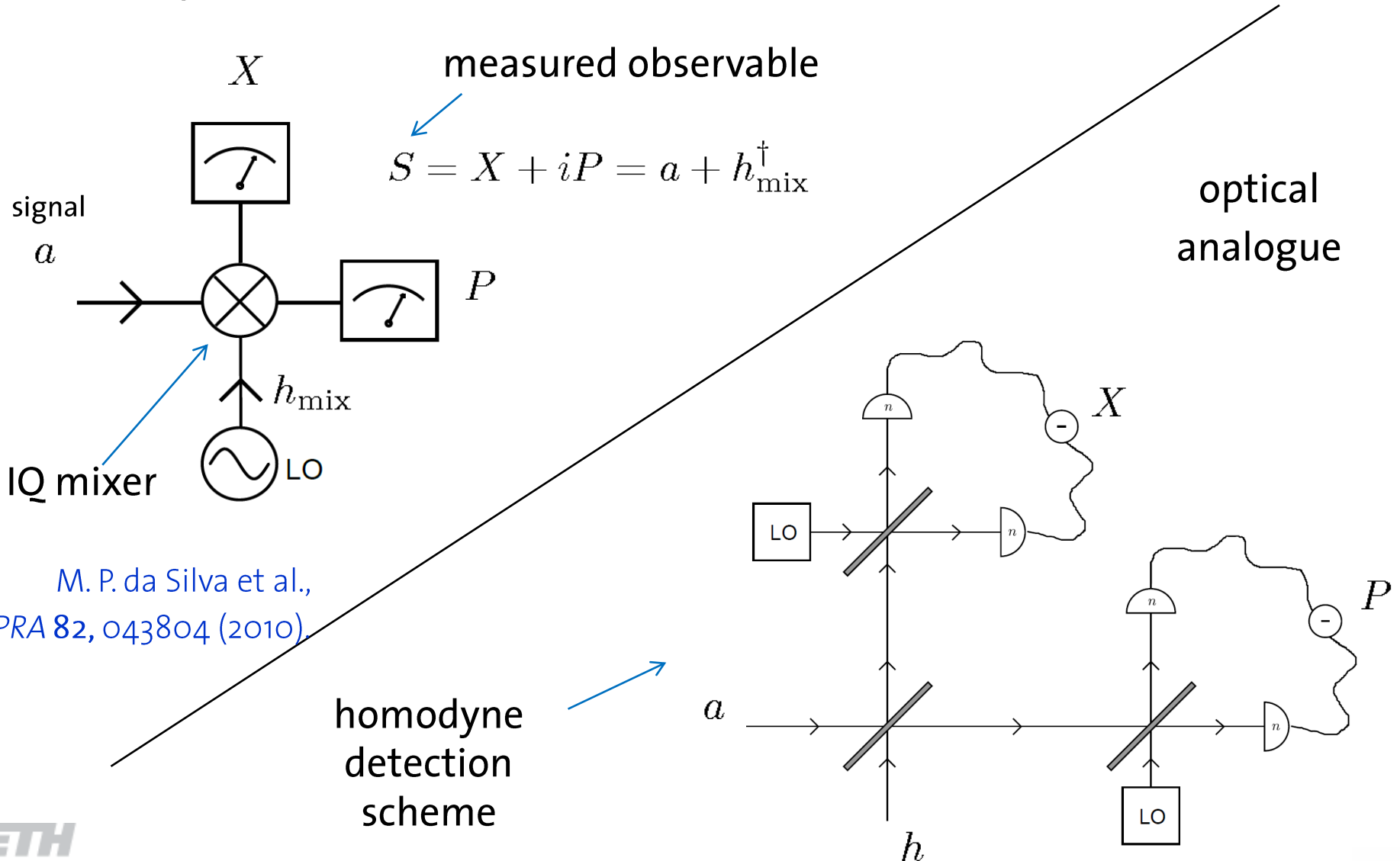
$a, b, h, \dots$  bosonic field operators

linear amplifier:



# ... and Quadrature Detectors

measuring field amplitude instead of photon number:



M. P. da Silva et al.,  
PRA 82, 043804 (2010).



# The Signal in One Channel of the Setup

signal mode  $a$  , vacuum mode  $v$

$$\rightarrow (a + iv)/\sqrt{2}$$

$$\rightarrow \sqrt{G/2}(a + iv) + \sqrt{G-1}h_{\text{amp}}^\dagger$$

$$\rightarrow \sqrt{G/2}(a + iv) + \underbrace{\sqrt{G-1}h_{\text{amp}}^\dagger + h_{\text{mix}}^\dagger}_{\propto h^\dagger}$$

$$\equiv \sqrt{G/2}(a + h^\dagger)$$

$$\equiv S = X + iP$$

effective noise mode

Beam splitter

Linear amplifier

Mixer

analogous for second channel!

# Statistics of Full Measurement Record

Extract electric field quadratures:

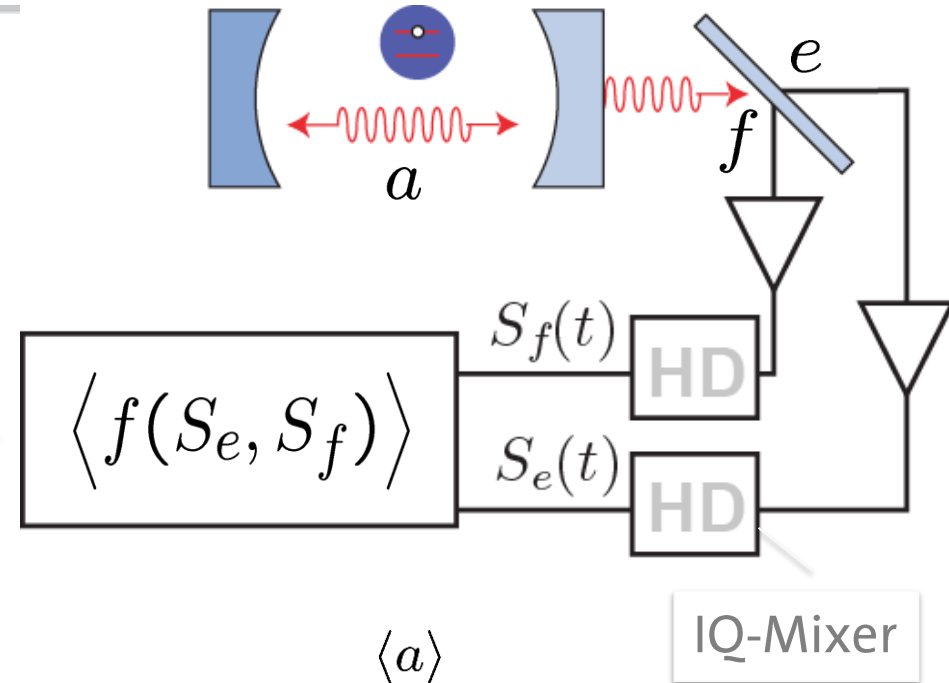
$$S_e(t) = X_e(t) + iP_e(t)$$

$$S_f(t) = X_f(t) + iP_f(t)$$

Real-time statistics  
in digital-electronics

Ensemble average finds:

- Quadratures  $\langle S_e \rangle$   $\langle a \rangle$
- Crosspower  $\langle S_e^* S_f \rangle$   $\langle a^\dagger a \rangle$
- Field correlation  $\langle S_e^*(t) S_f(t + \tau) \rangle$   $\langle a^\dagger(t) a(t + \tau) \rangle$
- Intensity correlation  $\langle S_e^*(t) S_e^* S_f(t + \tau) S_f(t) \rangle$   $\langle a^\dagger(t) n(t + \tau) a(t) \rangle$
- ... extract any correlation expressed in the cavity field operators



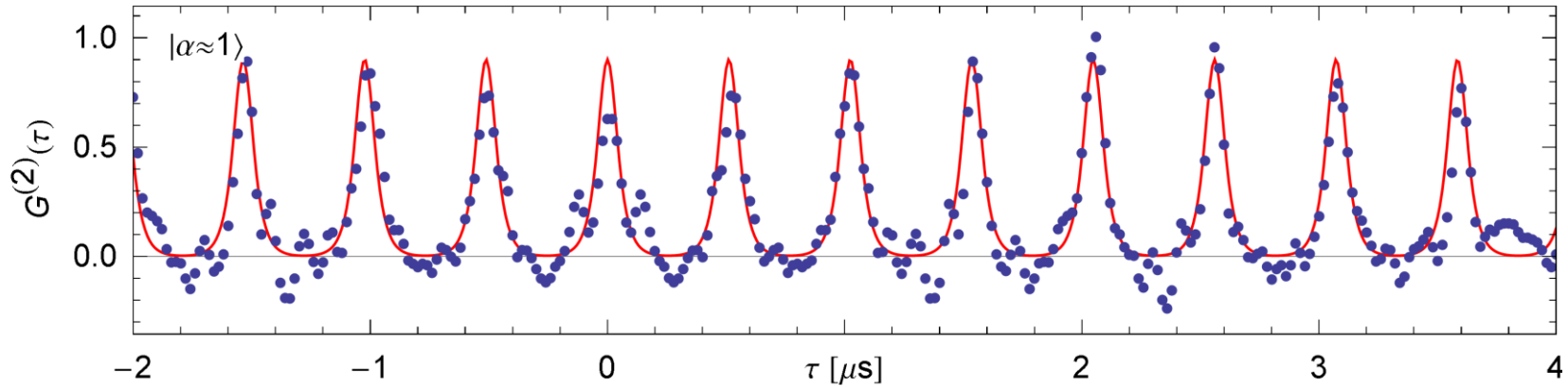
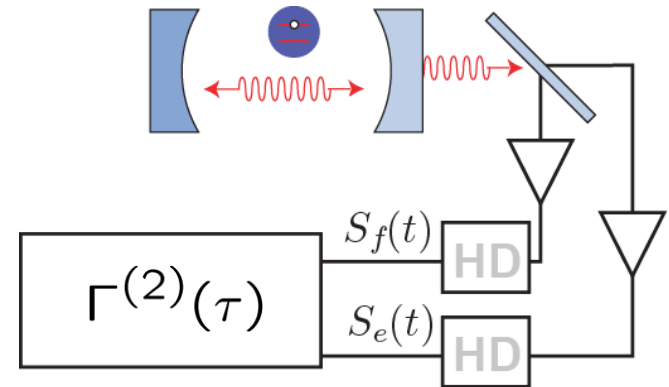
M. P. da Silva et al., *PRA* **82**, 043804 (2010)  
 D. Bozyigit et al., *Nat. Phys.* **7**, 154 (2011)  
 C. M. Caves, *Phys. Rev. D* **26**, 1817 (1982)  
 D. Walls and G. J. Milburn, Springer (2008)

# $G^{(2)}$ Measurement

Measure power correlation between channel e & f:

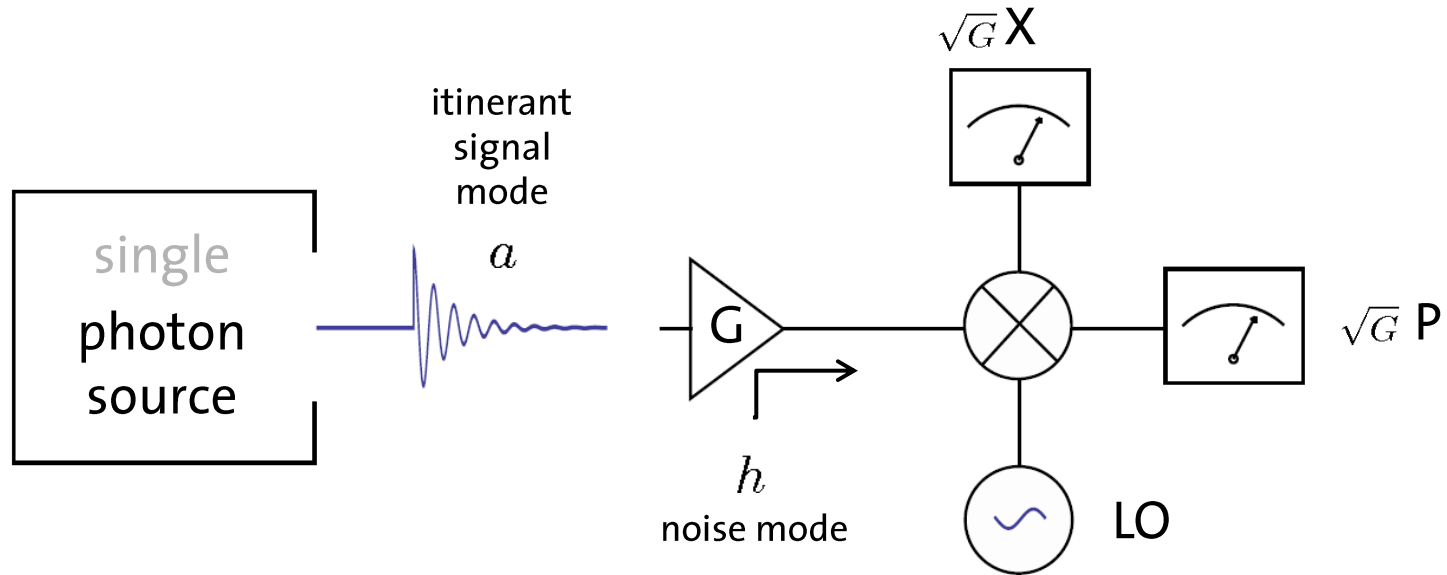
$$\Gamma^{(2)}(\tau) = \int \langle S_e^* S_f(t) S_e^* S_f(t + \tau) \rangle dt$$

$$G^{(2)}(\tau) = \Gamma_{prep}^{(2)}(\tau) - \Gamma_{ss}^{(2)}(\tau)$$



first  $G^{(2)}$  measurement for a microwave frequency single photon source

# Scheme for Tomography of Itinerant Photons



measured observable:  $X + iP = S = (a + h^\dagger)$

M. P. da Silva *et al.*,  
PRA 82, 043804 (2010)

What is the quantum state of mode  $a$  ?

**Goal:** Reconstruct density matrix, Wigner-, Q-, or P-function!





# Amplified Quadrature Histograms

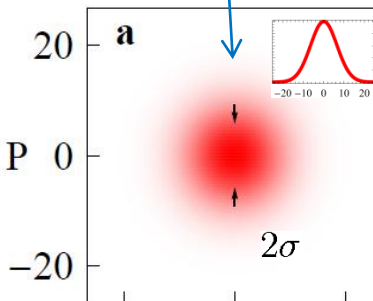
Store 2D histogram  $V(S)$  from  $S = X + iP$  measurement results:

corresponding phase space distribution

signal mode  $a$   
in vacuum

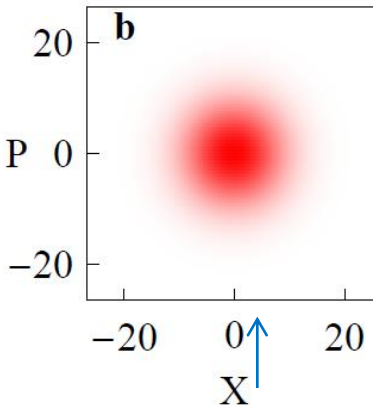
Q - function  
of noise mode :

$$Q_\eta$$

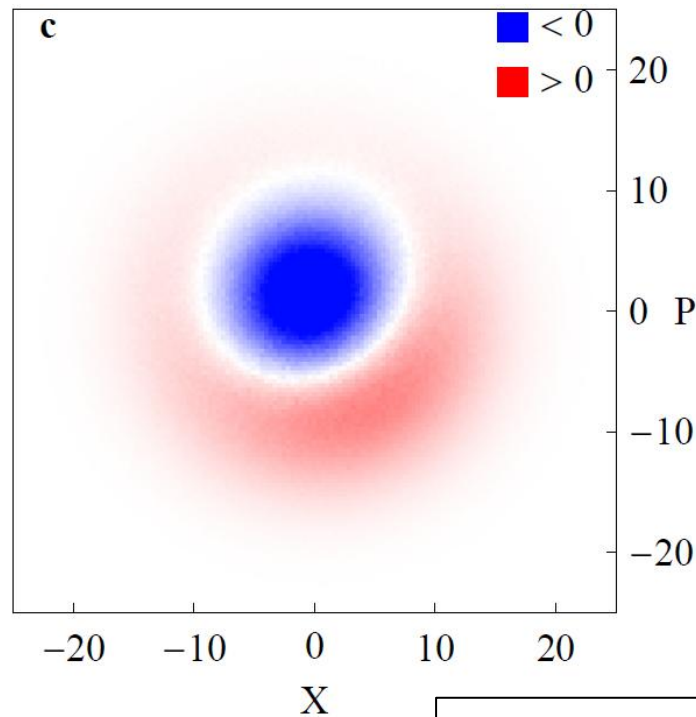


Convolution  
with P - function  
of signal

$$Q_\eta * P_a$$



signal mode  $a$   
in single photon  
Fock state



← subtracted  
histograms  
to visualize  
difference

separate noise  $\eta$  from  
signal  $a$  systematically!

C. Eichler et al., PRL 106, 220503 (2011)

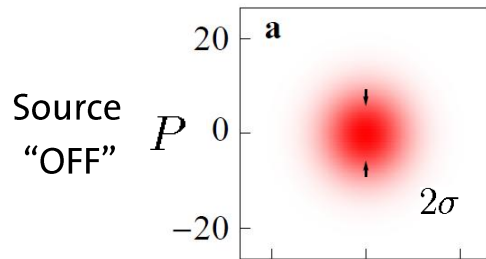
# Statistical Analysis of Phase Space Histograms

Systematic mode separation:

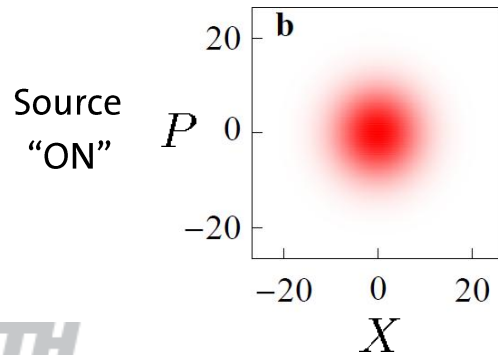
Histogram moments:  $\langle (S^\dagger)^n S^m \rangle = \int d^2S \ D(S) \ (S^*)^n S^m$

1. calculate histogram moments

2. algebraic inversion



$$\Rightarrow \langle (S^\dagger)^n S^m \rangle_{\text{OFF}} = \langle h^n (h^\dagger)^m \rangle$$



$$\Rightarrow \langle (S^\dagger)^n S^m \rangle_{\text{ON}} = \langle (a^\dagger + h)^n (a + h^\dagger)^m \rangle$$

$$\left. \begin{array}{l} \langle (S^\dagger)^n S^m \rangle_{\text{OFF}} \\ \langle (S^\dagger)^n S^m \rangle_{\text{ON}} \end{array} \right\} \langle (a^\dagger)^n a^m \rangle$$

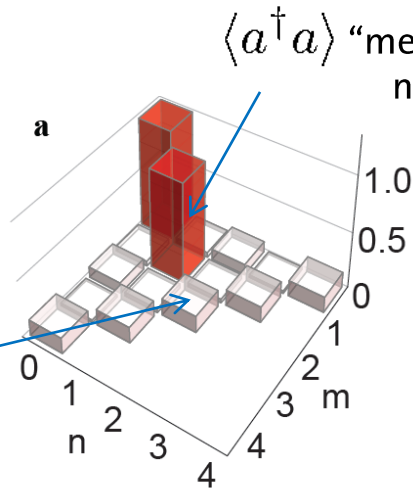
reminder:  $X + iP = S = (a + h^\dagger)$

# State Dependent Moments of Probability Distribution

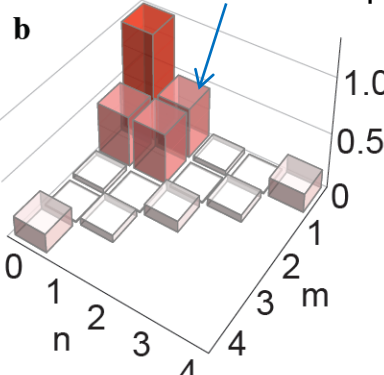
Moments  $\langle (a^\dagger)^n a^m \rangle$  for different prepared states:

Fock state

$$|1\rangle$$



$\langle a^\dagger a \rangle$  "mean photon number"

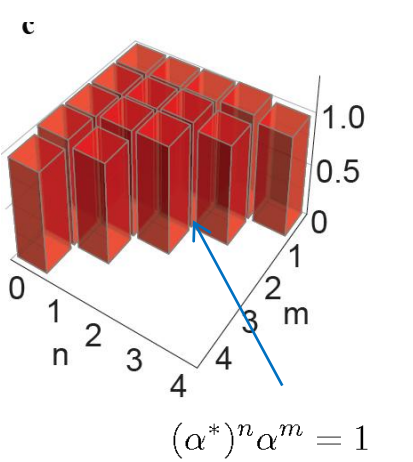


$\langle a^\dagger \rangle$  "mean amplitude"

superposition

$$\frac{1}{\sqrt{2}}(|0\rangle + e^{i\phi}|1\rangle)$$

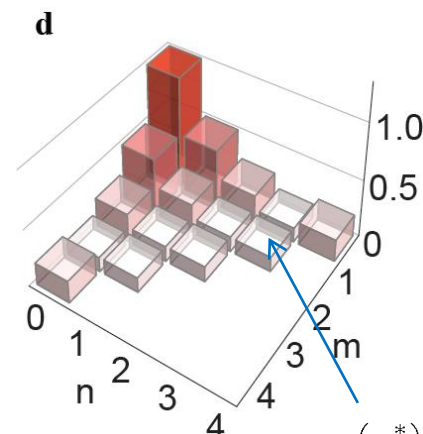
"anti bunching"



coherent state

$$|\alpha = 1\rangle$$

$$(\alpha^*)^n \alpha^m = 1$$



coherent state

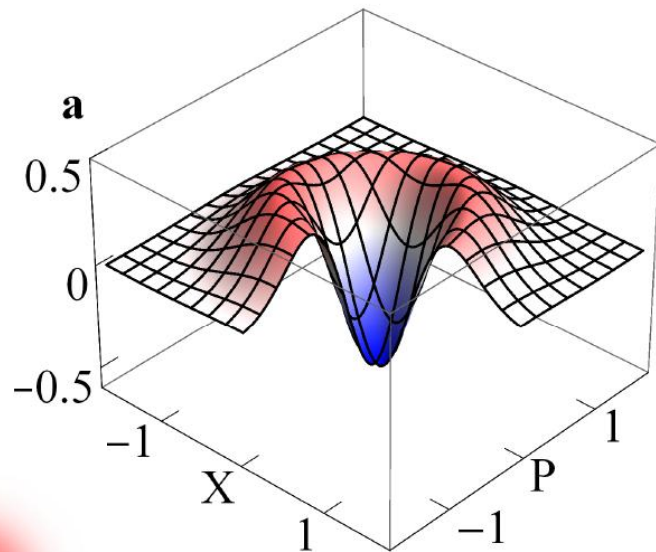
$$|\alpha = 0.5\rangle$$

$$(\alpha^*)^n \alpha^m = (1/2)^{n+m}$$

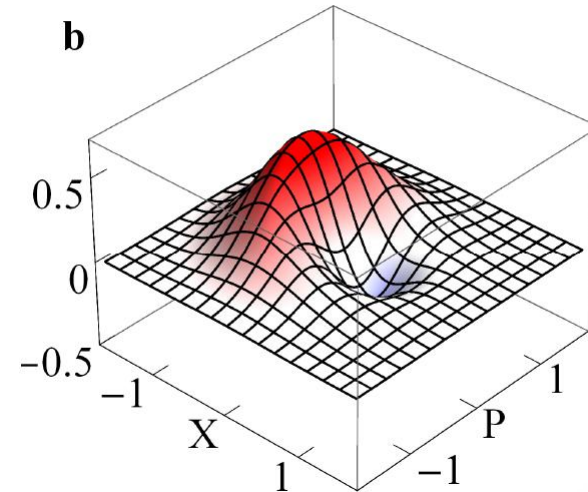
# Reconstructed Wigner Function of Itinerant Photon

Wigner function reconstructed from statistical moments:

$$W(\alpha) = \frac{1}{\pi^2} \sum_{n,m} \int d^2\lambda \frac{\langle (a^\dagger)^m a^n \rangle (-\lambda^*)^n \lambda^m}{n!m!} e^{-\frac{1}{2}|\lambda|^2 + \alpha\lambda^* - \alpha^*\lambda} \quad \text{with} \quad n + m < 4$$

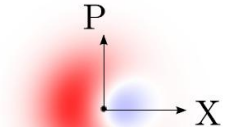
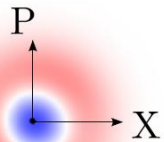


Fock state  
 $|1\rangle$



superposition

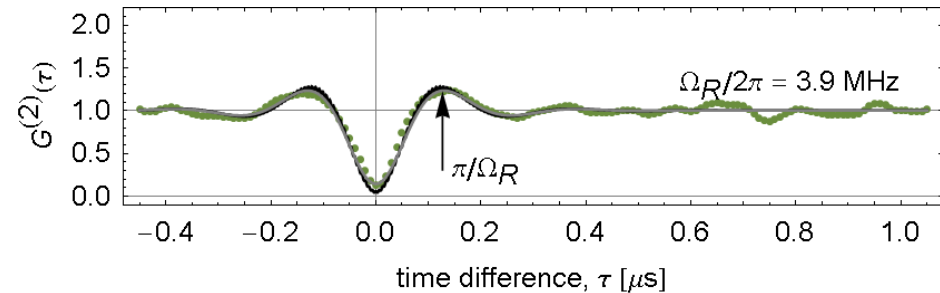
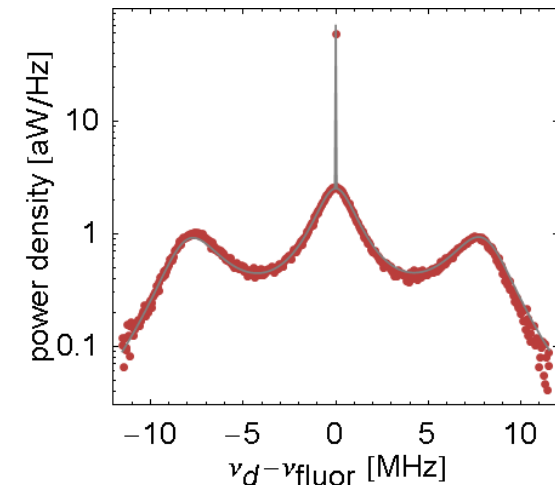
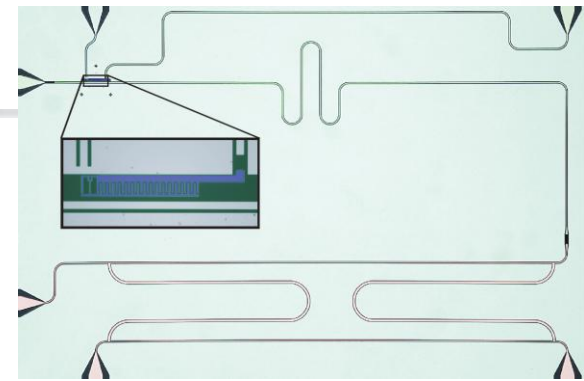
$$\frac{1}{\sqrt{2}}(|0\rangle + e^{i\phi}|1\rangle)$$





# Summary Correlations & Tomography

- ✓ realization of pulsed and continuously pumped microwave frequency single photon source
- ✓ implementation of on-chip beam splitter for correlation analysis
- ✓ characterization of single photon sources by:
  - ✓ time-resolved cavity field quadrature measurements
  - ✓ power, cross-power and photon number measurements
  - ✓ 1<sup>st</sup> and 2<sup>nd</sup> order two-time correlation functions

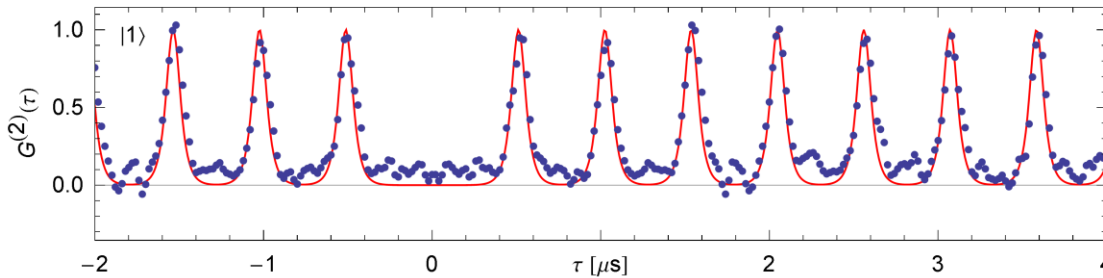


C. Lang *et al.*, *PRL* 106, 243601 (2011)

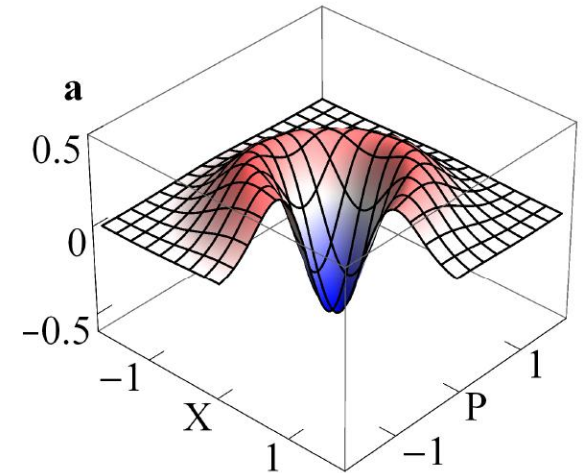
M. P. da Silva *et al.*, *PRA* 82, 043804 (2010)

# Summary Correlations & Tomography

- tomography of pulsed single photon sources ...
- ... and correlation function measurements



D. Bozyigit et al., *Nat. Phys.* 7, 154(2011)



C. Eichler et al., *PRL* 106, 220503 (2011)

- two mode squeezing generated using parametric amplifiers  
C. Eichler et al., *PRL* 107, 113601 (2011)
- **in the future:** do linear/non-linear optics in the circuit QED framework (e.g. realize photon/photon logic gates & interferometers)
- explore correlations at microwave frequencies in other systems
  - e.g. electron transport in nanostructures
- Demonstrated a great set of tools ready to be used in other fields!



# The ETH Zurich Quantum Device Lab

Postdoc and PhD positions available



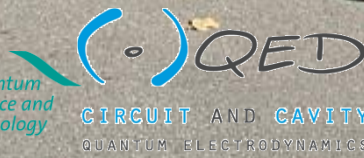
SWISS NATIONAL SCIENCE FOUNDATION



Eidgenössische Technische Hochschule Zürich  
Swiss Federal Institute of Technology Zurich



National Centre of Competence in Research



CIRCUIT AND CAVITY  
QUANTUM ELECTRODYNAMICS





# Selected Circuit QED Publications

## Circuit QED Proposal:

- Blais et al., *PRA* **69**, 062320 (2004)

## Strong Coupling & Vacuum Rabi Mode Splitting:

- Wallraff et al., *Nature* **431**, 162 (2004)
- Fink et al., *Nature* **454**, 315 (2008)
- Fink et al., *PRL* **105**, 163601 (2010)

## Tavis-Cummings Multi-Atom QED:

- Fink et al., *PRL* **103**, 083601 (2009)

## AC-Stark & Lamb Shift, Autler-Townes and Mollow Transitions

- Schuster et al., *PRL* **94**, 123062 (2005)
- Gambetta et al., *PRA* **74**, 042318 (2006)
- Schuster et al., *Nature* **445**, 515 (2007)
- Fragner et al., *Science* **322**, 1357 (2008)
- Baur et al., *PRL* **102**, 243602 (2009)

## Itinerant Photons, Tomography, Photon Blockade

- da Silva et al., *PRA* **82**, 043804 (2010)
- Bozyigit et al., *Nat. Phys.* **7**, 154 (2011)
- Eichler et al., *PRL* **106**, 220503 (2011)
- Lang et al., *PRL* **106**, 243601 (2011)
- Eichler et al., *PRL* **107**, 113601 (2011)

## One-, Two-, Three-Qubit Gates and Algorithms:

- Wallraff et al., *PRL* **95**, 060501 (2005)
- Blais et al., *PRA* **75**, 032329 (2007)
- Wallraff et al., *PRL* **99**, 050501 (2007)
- Majer et al., *Nature* **449**, 443 (2007)
- Leek et al., *Science* **318**, 1889 (2007)
- Leek et al., *PRB* **79**, 180511(R) (2009)
- Filipp et al., *PRL* **102**, 200402 (2009)
- Leek et al., *PRL* **104**, 100504 (2010)
- Bianchetti et al., *PRL* **105**, 223601 (2010)
- Fedorov et al., *Nature* **481**, 170 (2012)
- Baur et al., *PRL* **108**, 040502 (2012)

## Hybrid Systems:

- Frey et al., *PRL* **108**, 046807 (2012)
- Hogan et al., *PRL* **108**, 063004 (2012)

## Device Fabrication:

- Frunzio et al., *IEEE Trans. Appl. Sup.* **15**, 860 (2005)
- Goeppel et al., *J. Appl. Phys.* **104**, 113904 (2008)

## Review (gr.):

- Wallraff, *Physik Journal* **7 (12)**, 39 (Dez. 2008)

Additional Information: [www.qudev.ethz.ch](http://www.qudev.ethz.ch)